Example 1. The region R is in the first quadrant enclosed by the curves $y = 3x^2 - x^3$ and y = 0. Find the volume of the solid obtained by rotating R about the y-axis.

Example 2. The region R is in the first quadrant enclosed by the curves y = x and $y = x^3$. Use cylindrical shells, find the volume of the solid obtained by rotating R about the y-axis.

Example 3. The region R is enclosed by the curves $x = 2y^2 - y^3$ and x = 0. Use cylindrical shells, find the volume of the solid obtained by rotating R about the x-axis.

Example 4. Find the volume of the solid obtained by rotating the region bounded by $y = 2x - x^2$ and y = 0 about the line x = 3.

Example 5. The region R is in the first quadrant enclosed by the curves xy = 2, x = 0, y = 3, y = 4. Use cylindrical shells method to find the volume of the solid obtained by rotating R about the x-axis.