**Example 1.** Let S be a cone of radius r and height h. Show that the volume of S is  $V = \frac{1}{3}\pi r^2 h$ .

**Example 2.** Let S be a solid obtained by rotating about the x-axis the region under the curve  $y = \sqrt{x}$  from 0 to 2.

**Example 3.** Let S be a solid obtained by rotating about the y-axis the region bounded by  $y = x^4$  and y = 4.

**Example 4.** The region R is in the first quadrant enclosed by the curves y = x and  $y = x^3$ . Find the volume of the solid obtained by rotating R about the x-axis.

**Example 5.** Find the volume of the solid obtained by rotating the region in Example 4 about the line y = 2.

**Example 6.** Find the volume of the solid obtained by rotating the region in Example 4 about *y*-axis.

**Example 7.** Find the volume of the solid obtained by rotating the region in Example 4 about the line x = 1.