Example 1. Let $S$ be a cone of radius $r$ and height $h$. Show that the volume of $S$ is $V=\frac{1}{3} \pi r^{2} h$.

Example 2. Let $S$ be a solid obtained by rotating about the $x$-axis the region under the curve $y=\sqrt{x}$ from 0 to 2 .

Example 3. Let $S$ be a solid obtained by rotating about the $y$-axis the region bounded by $y=x^{4}$ and $y=4$.

Example 4. The region $R$ is in the first quadrant enclosed by the curves $y=x$ and $y=x^{3}$. Find the volume of the solid obtained by rotating $R$ about the $x$-axis.

Example 5. Find the volume of the solid obtained by rotating the region in Example 4 about the line $y=2$.

Example 6. Find the volume of the solid obtained by rotating the region in Example 4 about $y$-axis.

Example 7. Find the volume of the solid obtained by rotating the region in Example 4 about the line $x=1$.

